

- HORIE, H., HUSEBYE, S., KATO, M., MEYERS, E. A., MUTO, Y., SUZUKI, I., TOKII, T. & ZINGARO, R. A. (1986). *Acta Chem. Scand. Ser. A*, **40**, 579–589.
- HORIE, H., TOKII, T., MUTO, Y., STEWARD, O. W., CHANG, S.-C., SUZUKI, I., UEKUSA, H., OHBA, S., HUSEBYE, S. & KATO, M. (1992). In preparation.
- JOHNSON, C. K. (1971). ORTEPII. Report ORNL-3794. Oak Ridge National Laboratory, Tennessee, USA.
- KAHN, O. (1985). *Magneto-Structural Correlations in Exchange Coupled Systems*, edited by R. D. WILLET, D. GATTESCHI & O. KAHN, pp. 37–56. Dordrecht: D. Reidel.
- KATO, M. & MUTO, Y. (1988). *Coord. Chem. Rev.* **92**, 45–83.
- KAWATA, T., UEKUSA, H., OHBA, S., FURUKAWA, T., TOKII, T., MUTO, Y. & KATO, M. (1992). *Acta Cryst.* **B48**, 253–261.
- MORELAND, J. A. & DOEDENS, J. R. (1975). *J. Am. Chem. Soc.* **97**, 508–513.
- MORELAND, J. A. & DOEDENS, J. R. (1978). *Inorg. Chem.* **17**, 674–677.
- MUTO, Y., NAKASHIMA, M., TOKII, T., KATO, M. & SUZUKI, I. (1987). *Bull. Chem. Soc. Jpn.* **60**, 2849–2853.
- NAKASHIMA, M., MIKURIYA, M. & MUTO, Y. (1985). *Bull. Chem. Soc. Jpn.*, **58**, 968–973.
- PORTER, L. C., DICKMAN, M. H. & DOEDENS, R. J. (1986). *Inorg. Chem.* **25**, 678–684.
- SAKURAI, T. & KOBAYASHI, K. (1979). *Rikagaku Kenkyusho Hokoku*, **55**, 69–77.
- STEWARD, O. W., DZIEDZIC, J. E., JOHNSON, J. S. & FROHLIGER, J. O. (1971). *J. Org. Chem.* **36**, 3480–3484.
- STEWARD, O. W., KATO, M., CHANG, S. C., SAX, M., CHANG, C. H., JURY, C. F., MUTO, Y., TOKII, T., TAURA, T., PLETCHER, J. & YOO, C. S. (1991). *Bull. Chem. Soc. Jpn.* **63**, 3046–3058.
- STEWARD, O. W., MCAFEE, R. C., CHANG, S. C., PISKOR, S. R., SCHREIBER, W. J., JURY, C. F., TAYLOR, C. E., PLETCHER, J. F. & CHEN, C. S. (1986). *Inorg. Chem.* **25**, 771–777.
- UEKUSA, H., OHBA, S., SAITO, Y., KATO, M., STEWARD, O. W., TOKII, T. & MUTO, Y. (1990). *Acta Cryst.* **C46**, 1805–1812.
- YAMANAKA, M., UEKUSA, H., OHBA, S., SAITO, Y., IWATA, S., KATO, M., TOKII, T., MUTO, Y. & STEWARD, O. W. (1991). *Acta Cryst.* **B47**, 344–455.

*Acta Cryst.* (1992). **B48**, 667–672

## Electron-Density Distribution in Crystals of $lel_3-[M(chxn)_3](NO_3)_3 \cdot 3H_2O$ ( $M = Cr, Rh$ ; $chxn = trans\text{-}1,2\text{-diaminocyclohexane}$ ) at 120 K

BY MITSUO MOROOKA AND SHIGERU OHBA\*

*Department of Chemistry, Faculty of Science and Technology, Keio University, Hiyoshi 3-14-1, Kohoku-ku, Yokohama 223, Japan*

AND HIROSHI MIYAMAE

*Department of Chemistry, Faculty of Science, Josai University, Keyakidai 1-1, Sakado-shi, Saitama 350-02, Japan*

(Received 23 January 1992; accepted 13 April 1992)

### Abstract

The electron-density distributions in non-centrosymmetric crystals containing  $Cr^{III}$  or  $Rh^{III}$  complexes with *trans*-1,2-diaminocyclohexane (*chxn*) as a bidentate ligand have been investigated by the multipole expansion method based on X-ray intensities collected at 120 K with Mo  $K\alpha$  radiation ( $\lambda = 0.71073 \text{ \AA}$ ). Crystals of the  $Cr^{III}$  and  $Rh^{III}$  complexes are isomorphous and hexagonal  $P6_3$ ,  $Z = 2$ . (I):  $\Delta(\lambda\lambda\lambda)$ -tris(*trans*-1,2-diaminocyclohexane)-chromium(III) nitrate trihydrate,  $[Cr(C_6H_{14}N_2)_3](NO_3)_3 \cdot 3H_2O$ ,  $M_r = 634.6$ ,  $F(000) = 678$ ,  $a = 13.029(2)$ ,  $c = 10.040(2) \text{ \AA}$ ,  $V = 1476.0(5) \text{ \AA}^3$ ,  $D_x = 1.43 \text{ Mg m}^{-3}$ ,  $\mu = 0.444 \text{ mm}^{-1}$ ,  $R = 0.041$  for 3914 reflections. (II):  $\Delta(\lambda\lambda\lambda)$ -tris(*trans*-1,2-diaminocyclohexane)rhodium(III) nitrate trihydrate,  $[Rh(C_6H_{14}N_2)_3](NO_3)_3 \cdot 3H_2O$ ,  $M_r = 685.5$ ,  $F(000) = 720$ ,  $a = 13.101(2)$ ,  $c = 9.984(2) \text{ \AA}$ ,  $V =$

$1484.0(5) \text{ \AA}^3$ ,  $D_x = 1.53 \text{ Mg m}^{-3}$ ,  $\mu = 0.632 \text{ mm}^{-1}$ ,  $R = 0.028$  for 4602 reflections. The electron populations of the  $d$  orbitals of  $Cr^{III}$  and  $Rh^{III}$  atoms in a chemical  $D_3$  ligand field were estimated and compared with those of the  $lel_3\text{-Co}^{III}$  complex. Phase improvement is necessary even when the valence/core-electron ratio becomes smaller, because the phases based on the independent atom model are poor for one of the hexadecapole densities of the metal atoms in the title crystals.

### Introduction

It is well-known that deformation densities of non-centrosymmetric structures suffer from phase error and the features are much smeared if the phase angle of  $F_o$  is estimated based on the spherical independent atom model (IAM). This inadequacy can be removed by the aspherical-atom model (Hirshfeld, 1971). In a previous paper (Morooka, Ohba, Saito & Miyamae,

\* To whom correspondence should be addressed.

Table 1. Experimental information for (A) conventional and (B) multipole refinements

	Cr		Rh	
	A	B	A	B
No. of reflections	3914	3914	4602	4602
No. of parameters	184	319	184	319
$R(F)$	0.048	0.041	0.031	0.028
$wR(F)$	0.037	0.028	0.030	0.025
$S$	1.25	0.97	1.17	0.99

1991), phase improvement for  $lel_3$ - and  $ob_3$ - $[Co(chxn)_3](NO_3)_3 \cdot 3H_2O$  crystals was carried out by the multipole expansion method. Unexpectedly, it was found that the effect of phase improvement on the deformation densities around the Co atoms is anisotropic. This peculiarity was rationalized by considering the contributions of two hexadecapole densities,  $\rho_{40}$  and  $\rho_{43-}$ , to the structure factors. In the present study,  $lel_3$ - $[M(chxn)_3](NO_3)_3 \cdot 3H_2O$  ( $M = Cr, Rh$ ) crystals have been examined in order to investigate the necessity of phase improvement for metal atoms with a lower valence-/core-electron ratio than for the Co atom. The  $Cr^{III}$ ,  $Co^{III}$  and  $Rh^{III}$  crystals are isostructural, and the metal atoms lie on a crystallographic threefold axis. Crystal structure analysis and a preliminary study of the electron-density distribution in  $lel_3$ - and  $ob_3$ - $Rh^{III}$  complexes has already been carried out at room temperature (Miyamae, Sato & Saito, 1977; Miyamae, 1977).

Preparation, separation and characterization of the  $[Cr(chxn)_3]^{3+}$  (Harnung & Laier, 1978) and  $[Rh(chxn)_3]^{3+}$  (Galsbøl, Steenbøl & Sørensen, 1972) complexes have been reported as well as those of the  $Co^{III}$  complexes (Harnung, Sørensen, Creaser, Mægaard, Pfenninger & Schäffer, 1976), and the  $Ir^{III}$  systems (Galsbøl, 1978).

## Experimental

### Data collection

Crystals of  $\Delta(\lambda\lambda\lambda)-[M(R,R\text{-}chxn)_3](NO_3)_3 \cdot 3H_2O$  ( $M = Cr, Rh$ ) were kindly supplied by Dr F. Galsbøl of the H. C. Ørsted Institute, University of Copenhagen.

(I): An orange hexagonal prismatic crystal of the Cr complex was shaped into a sphere of 0.56 (1) mm in diameter and mounted on a Rigaku AFC-5 four-circle diffractometer. Data collection was carried out with graphite-monochromatized Mo  $K\alpha$  radiation at 120 (2) K by using a nitrogen-gas-flow cooling unit.  $\theta$ - $2\theta$  scan technique was adopted with scan speed  $6^\circ \text{ min}^{-1}$  in  $\theta$  and scan width  $(1.3 + 0.36 \tan \theta)^\circ$ . Range of indices,  $-18 \leq (h,k) \leq 18$ ,  $0 \leq l \leq 14$  ( $4 < 2\theta \leq 60^\circ$ );  $0 \leq (h,k) \leq 28$ ,  $0 \leq l \leq 21$  ( $60 < 2\theta \leq 100^\circ$ ). Five standard reflections showed no significant variation,  $0.995 < |F_o|/|F_o|_{\text{initial}} < 1.009$ . 13 162 reflections were measured, 11 011 reflections were observed with

Table 2. Positional parameters ( $\times 10^4$ ) and equivalent isotropic temperature factors

Compound (I)	$B_{eq} = (8\pi^2/3) \sum_i \sum_j U_{ij} a_i^* a_j^* a_i \cdot a_j$			$B_{eq} (\text{\AA}^2 \times 10)$
	$x$	$y$	$z$	
Cr	3333	6667	0	7 (1)
N(1)	2193 (1)	5228 (1)	-1196 (1)	9 (1)
N(2)	3297 (1)	5354 (1)	1196 (1)	9 (1)
C(1)	2388 (1)	4228 (1)	-824 (1)	11 (1)
C(2)	2367 (1)	4173 (1)	690 (1)	11 (1)
C(3)	2529 (1)	3166 (1)	1204 (2)	21 (1)
C(4)	1604 (2)	1981 (1)	592 (3)	30 (1)
C(5)	1673 (2)	2049 (1)	-947 (2)	26 (1)
C(6)	1480 (1)	3051 (1)	-1435 (2)	16 (1)
N(3)	5945 (1)	5129 (1)	946 (1)	13 (1)
O(1)	5526 (1)	5367 (1)	1936 (1)	25 (1)
O(2)	5655 (1)	5264 (1)	-215 (1)	18 (1)
O(3)	6631 (1)	4723 (1)	1100 (1)	21 (1)
O(W)	7970 (1)	5066 (1)	-1321 (2)	19 (1)
Compound (II)				
Rh	3333	6667	0	8 (1)
N(1)	2168 (1)	5245 (1)	-1179 (1)	11 (1)
N(2)	3339 (1)	5377 (1)	1188 (1)	11 (1)
C(1)	2370 (2)	4251 (1)	-825 (2)	12 (1)
C(2)	2394 (2)	4205 (2)	694 (2)	14 (1)
C(3)	2550 (2)	3197 (1)	1195 (2)	24 (1)
C(4)	1618 (3)	2021 (2)	595 (4)	33 (1)
C(5)	1635 (3)	2080 (2)	-939 (3)	31 (1)
C(6)	1448 (1)	3080 (1)	-1417 (2)	19 (1)
N(3)	5947 (1)	5126 (1)	947 (1)	16 (1)
O(1)	5558 (1)	5399 (2)	1933 (2)	31 (1)
O(2)	5652 (1)	5246 (1)	-220 (2)	22 (1)
O(3)	6610 (1)	4706 (1)	1112 (1)	23 (1)
O(W)	7950 (1)	5057 (1)	-1330 (2)	23 (1)

$|F_o| > 3\sigma(|F_o|)$ , and 3914 unique reflections were obtained ( $R_{\text{int}} = 0.017$ ). Lattice constants were determined based on 25  $2\theta$  values ( $22 < 2\theta < 32^\circ$ ). Analytical corrections for absorption were made with  $\mu r = 0.124$  assuming a spherical crystal shape (transmission factors  $0.831 < A < 0.834$ ).

(II): Crystals of the Rh complex are colorless hexagonal prisms. Intensity data were collected at 120 (2) K using a spherical crystal 0.56 (2) mm in diameter. Range of indices,  $-18 \leq (h,k) \leq 18$ ,  $0 \leq l \leq 14$  ( $4 < 2\theta \leq 60^\circ$ );  $0 \leq (h,k) \leq 28$ ,  $0 \leq l \leq 21$  ( $60 < 2\theta \leq 100^\circ$ ). There was no significant variation of five

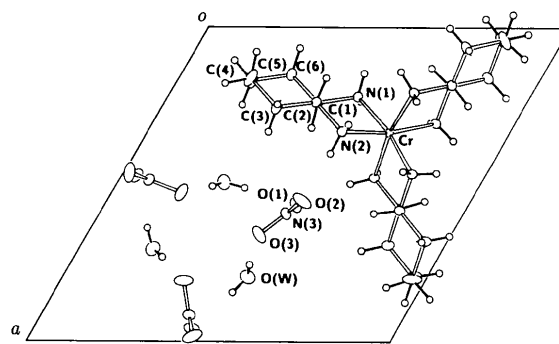


Fig. 1. Partial projection of the crystal structure of the Cr complex along the  $c$  axis.

Table 3. Bond lengths (Å) and bond angles (°)

	Cr	Rh
M—N(1)	2.092 (1)	2.084 (1)
M—N(2)	2.071 (1)	2.068 (1)
N(1)—C(1)	1.494 (2)	1.495 (3)
N(2)—C(2)	1.493 (1)	1.494 (2)
C(1)—C(2)	1.521 (1)	1.519 (3)
C(1)—C(6)	1.521 (2)	1.519 (2)
C(2)—C(3)	1.520 (2)	1.518 (4)
C(3)—C(4)	1.534 (2)	1.530 (3)
C(4)—C(5)	1.548 (4)	1.533 (5)
C(5)—C(6)	1.528 (3)	1.525 (4)
N(3)—O(1)	1.246 (2)	1.241 (3)
N(3)—O(2)	1.264 (2)	1.262 (2)
N(3)—O(3)	1.255 (2)	1.250 (2)
N(1)—M—N(2)	83.10 (5)	83.90 (5)
M—N(1)—C(1)	106.5 (1)	106.0 (1)
M—N(2)—C(2)	109.0 (1)	108.1 (1)
N(1)—C(1)—C(2)	106.5 (1)	106.7 (2)
N(1)—C(1)—C(6)	113.1 (1)	112.9 (2)
C(2)—C(1)—C(6)	111.6 (1)	111.7 (1)
N(2)—C(2)—C(1)	107.8 (1)	108.2 (1)
N(2)—C(2)—C(3)	112.5 (1)	112.5 (2)
C(1)—C(2)—C(3)	111.9 (1)	112.2 (2)
C(2)—C(3)—C(4)	110.8 (1)	111.1 (2)
C(3)—C(4)—C(5)	110.4 (1)	110.9 (2)
C(4)—C(5)—C(6)	109.8 (2)	110.6 (3)
C(1)—C(6)—C(5)	110.8 (1)	111.0 (2)
O(1)—N(3)—O(2)	120.2 (1)	120.1 (2)
O(1)—N(3)—O(3)	120.0 (1)	119.9 (2)
O(2)—N(3)—O(3)	119.8 (1)	120.0 (2)

standard reflections,  $0.995 < |F_o|/|F_o|_{\text{initial}} < 1.005$ . 13 235 reflections were measured, 12 061 reflections were observed with  $|F_o| > 3\sigma(|F_o|)$ , and 4602 unique reflections were obtained ( $R_{\text{int}} = 0.011$ ). Absorption corrections with  $\mu r = 0.177$  were made ( $0.769 < A < 0.774$ ).

### Refinement

At first, conventional refinement was attempted using the full-matrix least-squares program *MOLLY* (Hansen & Coppens, 1978) without multipoles (refinement *A*). As the extinction effect was negligible, subsequent refinements were carried out without an extinction correction. Scattering factors of core and valence shells of non-H atoms were taken from *International Tables for X-ray Crystallography* (1974, Vol. IV). For H atoms, scattering factors were those of Stewart, Davidson & Simpson (1965). The function  $\sum w(|F_o| - |F_c|)^2$  was minimized with weights  $w^{-1} = \sigma^2(|F_o|) + (0.015|F_o|)^2$ . Refinement information is listed in Table 1. The structural chirality was assigned with reference to the known absolute configuration of the ligand, (–)-*R,R*-chxn (Miyamae, Sato & Saito, 1977). For the enantiomeric structures, the *R* values increased:  $R = 0.051$  and  $wR = 0.041$  for Cr, and  $R = 0.032$  and  $wR = 0.031$  for the Rh crystal.

In refinement *B*, multipoles were included up to the hexadecapole level for all non-H atoms. The radial functions are  $r^n \exp(-\zeta r)$  with  $n_l = 4$  for all *l* values (Cr, Rh) and  $n_l = 2, 2, 2, 3, 4$  for  $l = 0, 1, 2, 3,$

Table 4. Hydrogen-bond lengths (Å) involving the ligating N atoms

	Cr	Rh
N(1)⋯O(2 <sup>i</sup> )	3.123 (2)	3.116 (2)
N(1)⋯O(3 <sup>ii</sup> )	3.102 (2)	3.127 (2)
N(2)⋯O(1)	2.990 (2)	2.987 (2)
N(2)⋯O(W <sup>iii</sup> )	2.887 (2)	2.891 (2)

Symmetry codes: (i)  $-x + y, 1 - x, z$ ; (ii)  $1 - x, 1 - y, z - \frac{1}{2}$ ; (iii)  $1 - x, 1 - y, z + \frac{1}{2}$ .

Table 5. Electron populations for the metal *d* orbitals

	Cr	Co*	Rh
Total	3.42 (7)	5.98 (8)	7.12 (12)
<i>a<sub>1</sub></i>	0.95 (5)	1.71 (6)	1.90 (6)
<i>e</i>	1.87 (10)	3.12 (12)	3.83 (13)
<i>e'</i>	0.60 (10)	1.15 (12)	1.39 (13)
<i>e, e', + e-e'</i>	0.55 (12)	0.23 (14)	0.40 (15)

\* Morooka, Ohba, Saito & Miyamae (1991).

4 (O, N and C). The positional, thermal, multipole and  $\zeta$  (shielding) parameters were refined. Initial  $\zeta$  values were taken from Clementi & Raimondi (1963) for Cr, O, N and C atoms and that for Rh was obtained assuming the shielding-constants rule proposed by Slater (see Eyring, Walter & Kimball, 1944). The 4*s* and 4*p* orbital populations of Cr and the 5*s* and 5*p* orbital populations of Rh were not taken into account. Chemical symmetry 32 ( $D_3$ ) of the complex cation was assumed. Symmetry constraints on the multipole parameters were imposed upon  $\text{NO}_3^-$  ( $D_{3h}$ ) and  $\text{H}_2\text{O}$  ( $C_{2v}$ ) in order to reduce the number of multipole parameters. The total charge of the unit cell was constrained to be neutral. For H atoms, no multipoles were introduced and the valence-electron populations were fixed at unity in order to avoid an unrealistic result. Partial projections of the crystal structures are presented in Fig. 1 together with the atom-numbering scheme. Atomic coordinates are listed in Table 2, and bond lengths and angles in Table 3.\* Hydrogen-bond lengths involving the ligating N atoms are listed in Table 4.

Electron populations of the Cr and Rh *d* orbitals are listed in Table 5 and were derived from the multipole coefficients (Holladay, Leung & Coppens, 1983). Equations giving the orbital populations as linear combinations of the multipole parameters are contained in the previous paper (Morooka, Ohba, Saito & Miyamae, 1991). Computations were carried out on a MIPS RS3230 Workstation.

\* Lists of structure factors, anisotropic thermal parameters, positional parameters of H atoms, bond lengths and bond angles involving H atoms, and multipole parameters have been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 55158 (31 pp.). Copies may be obtained through The Technical Editor, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England. [CIF reference: AS0599]

## Discussion

### Phase improvement

Deformation density maps around the Cr and Rh atoms after multipole refinement are shown in Fig. 2 and were calculated as the difference densities between the observed electron-density distribution and the superposition of those for spherical atoms with refined effective charges in order to show the charge asphericity around the metal atoms clearly. Deformation density maps calculated after conventional refinement are shown in Fig. 3. The negative

troughs located perpendicular to the  $M-N$  bond in Fig. 3 disappeared after phase improvement (Fig. 2). This phenomenon was also found for the  $lel_3-Co^{III}$  complex (Morooka, Ohba, Saito & Miyamae, 1991). The deformation densities around the metal atoms mainly consist of the hexadecapole densities  $\rho_{40}$  and  $\rho_{43-}$ . The positive peaks on the threefold axis ( $z$ ) correspond to  $\rho_{40}$  and the negative troughs on the  $M-N$  bond axes and positive peaks on the pseudo-threefold axes of the  $MN_6$  octahedron correspond to both  $\rho_{40}$  and  $\rho_{43-}$ . From the phase errors based on the independent atom model (IAM), the features of  $\rho_{43-}$  are smeared and those of  $\rho_{40}$  remain [see Fig. 6

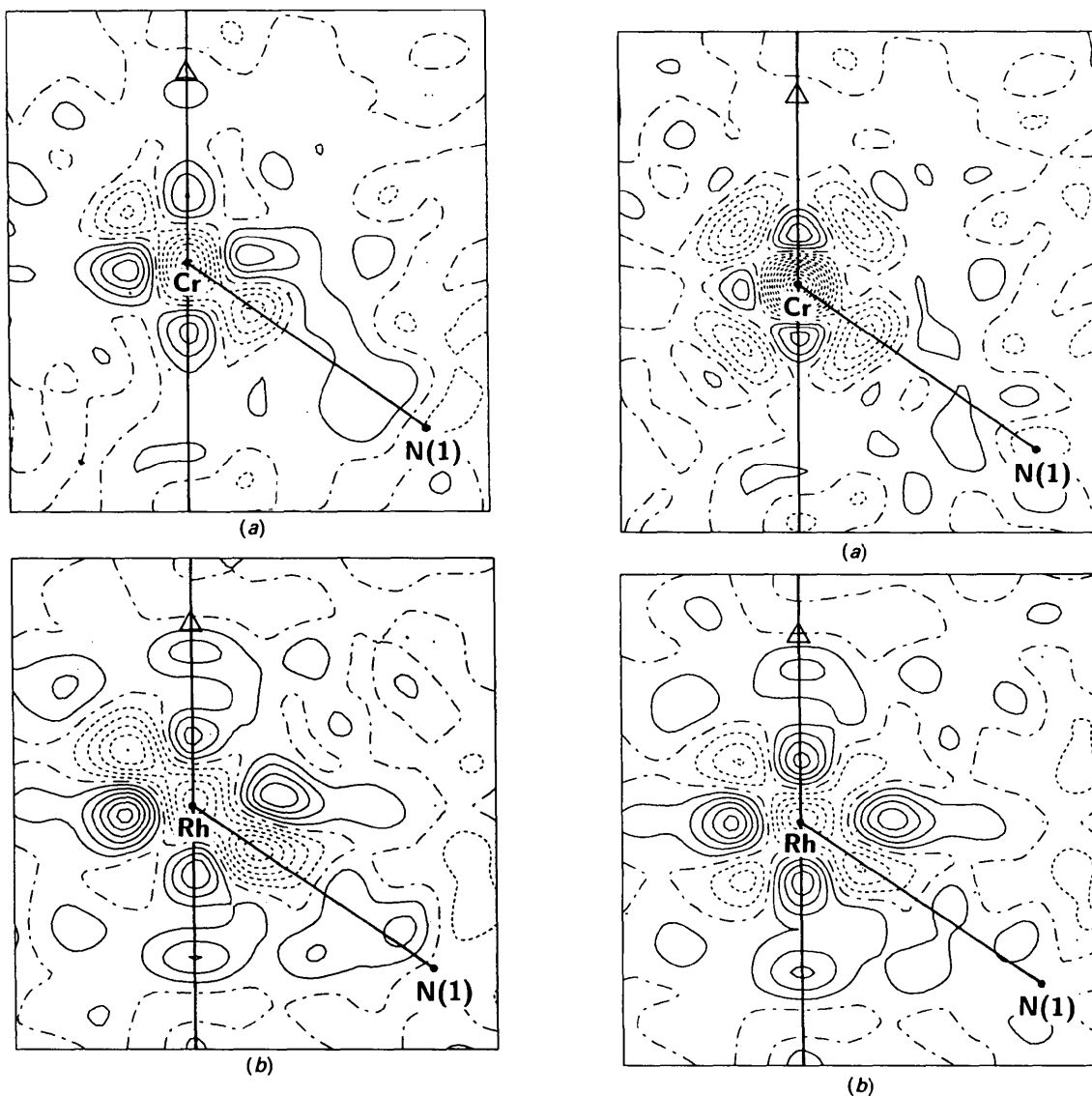


Fig. 2. Observed deformation density after phase improvement for (a) Cr and (b) Rh complexes. This is a section through an  $M-N$  bond and the threefold axis. Contour intervals at  $0.2 e \text{ \AA}^{-3}$ . The standard deviations are (a) 0.09 and (b)  $0.10 e \text{ \AA}^{-3}$  in the general position.

Fig. 3. Difference Fourier synthesis after conventional refinement (including phase error) for (a) Cr and (b) Rh complexes. The planes shown are the same as in Fig. 2. Contour intervals at  $0.2 e \text{ \AA}^{-3}$ .

of Morooka, Ohba, Saito & Miyamae (1991)]. In order to understand this phenomenon, we consider  $F_{40}$  and  $F_{43-}$ , the contributions of  $\rho_{40}$  and  $\rho_{43-}$  to the structure factors. The phases of  $F_{40}$  and  $F_{43-}$  are limited to  $n\pi/2$  depending on the parity of the reflection index  $l$  and on the parity of the multipole density to a rotation around  $z$  of  $180^\circ$ , as a result of the arrangement of the Co atoms in the unit cell [see Table 5 of Morooka, Ohba, Saito & Miyamae (1991)]. For the reflections to which the contribution of the metal atom is dominant, the phase of IAM is a good approximation to  $F_{00}$  (valence monopole) and  $F_{40}$ , but not explicitly for  $F_{43-}$ . For example, when  $l$

is even,  $F_{00}$  and  $F_{40}$  are real. On the other hand,  $F_{43-}$  is purely imaginary. This is the reason why the phase improvement for  $\rho_{43-}$  is still significant when the valence-/core-electron ratio becomes smaller for  $\text{Cr}^{\text{III}}$  and  $\text{Rh}^{\text{III}}$  complexes.

#### Charge asphericity

Dynamic multipole-model deformation density maps at the experimental resolution ( $\sin\theta/\lambda \leq 1.08 \text{ \AA}^{-1}$ ) are shown in Fig. 4, where the contributions of the unobserved reflections were supplemented. There are typical  $d$ -electron distributions in the approximately  $O_h$  ligand field. As seen from

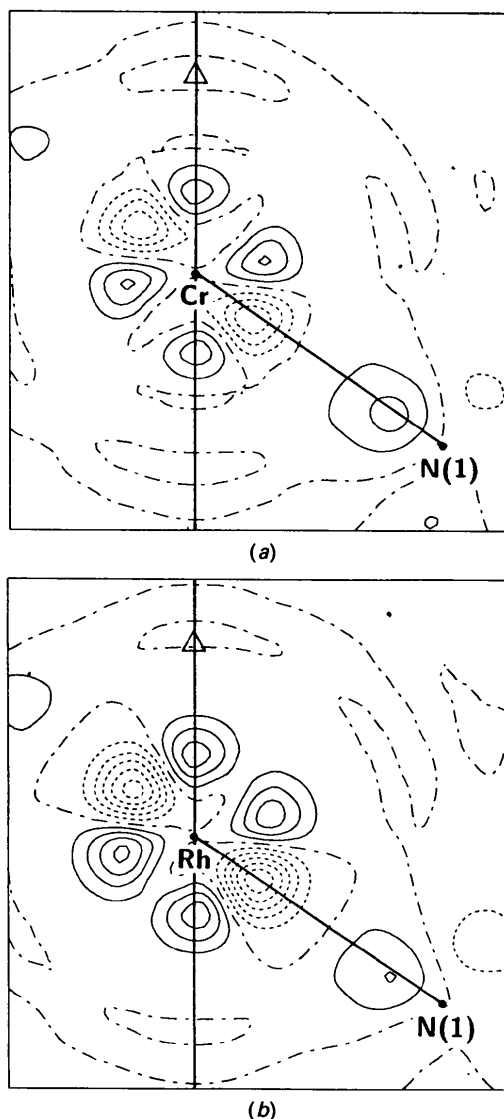


Fig. 4. Model deformation density based on all reflections within the range  $\sin\theta/\lambda \leq 1.08 \text{ \AA}^{-1}$  for (a) Cr complex with 5348 reflections and (b) Rh complex with 5382 reflections. The planes are the same as shown in Fig. 2. Contour intervals at  $0.2 \text{ e \AA}^{-3}$ .

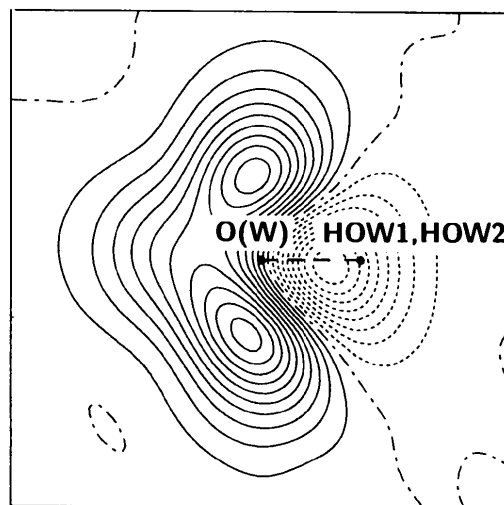


Fig. 5. Model deformation density in the plane bisecting the H—O—H bond angle and perpendicular to the  $\text{H}_2\text{O}$  molecule in the Cr crystal,  $\sin\theta/\lambda \leq 1.08 \text{ \AA}^{-1}$ . Contour intervals at  $0.05 \text{ e \AA}^{-3}$ . The two hydrogen atoms HOW1 and HOW2 are shifted from the plane by  $\pm 0.64 \text{ \AA}$ .

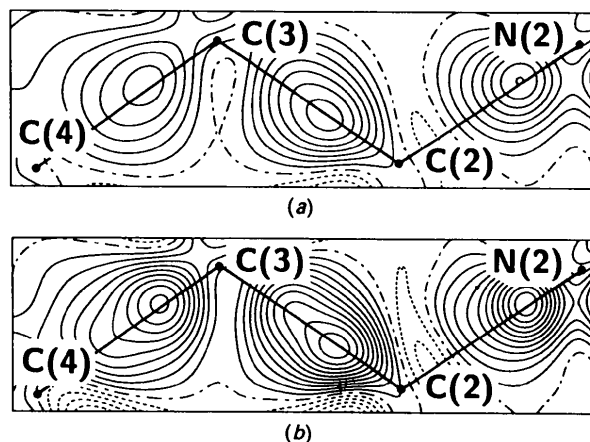


Fig. 6. (a) Dynamic and (b) static model deformation density in the plane containing the  $\text{N}(2)\text{—C}(2)\text{—C}(3)$  bond axes of the Cr complex,  $\sin\theta/\lambda \leq 1.08 \text{ \AA}^{-1}$ . Contour intervals at  $0.05 \text{ e \AA}^{-3}$ .

Table 5, the ratios of the electron populations in the  $a_1$  and  $e$  orbitals of the  $lel_3-[M(chxn)_3]^{3+}$  ( $M = Cr, Co$  and  $Rh$ ) complexes are 1:2 within experimental error. This accords with the fact that the coordination geometry around the metal atoms is nearly octahedral. The inclination angles of the  $M-N$  bond axes to the threefold axis are 54.57 (4)–54.98 (3), 54.23 (4)–54.55 (3) and 55.00 (4)–55.61 (3)° for  $lel_3-Cr, Co$  and  $Rh$  complexes, respectively. The corresponding angle for a regular octahedron is 54.74°. In the  $Co^{III}$  complex with the macrocyclic ligand hexaen (1,4,7,10,13,16-hexaazacyclooctadecane), the  $Co-N$  inclination angle is 59.312 (6)° and the population of the  $a_{1g}$  orbital is larger [by 9 (2)%] than that of the  $e_g$  orbitals, suggesting the lowest ligand field in the threefold axis (Morooka, Ohba & Toriumi, 1992). Comparing this result with the  $Co^{III}$  and  $Rh^{III}$  complexes, the asphericities in the 3d- and 4d-electron distributions seem to be essentially identical. A significant imbalance in the  $M-N$  bond lengths was observed for the series of  $[M(chxn)_3](NO_3)_3 \cdot 3H_2O$  crystals; however, it does not seem to be as a result of the hydrogen bonds (see Table 4).

The model deformation density map in the  $NO_3^-$  plane in the  $Cr$  crystal indicated the  $N-O$  bonding electrons and oxygen lone-pair electrons as was similarly observed in the  $Co$  crystal. The model deformation density in the plane bisecting the  $H-O-H$  bond angle is shown in Fig. 5. Lone-pair electrons of the  $O$  atom are observed as an elongated peak with double maxima. Fig. 6(a) is the model deformation density map of the  $chxn$  ligand in which the  $C-C$  and  $C-N$  bonding electrons are observed. The subtracted promolecule for Fig. 6 is the independent atom model with neutral atomic charges in order to

compare the peak heights based on the same reference atomic densities. The density on the  $C(3)-C(4)$  axis is lower than that on the  $C(2)-C(3)$  axis because of the larger thermal vibration of the  $C(4)$  atom, which is further from the metal center than  $C(2)$ . The peak heights on the  $C(2)-C(3)$  and  $C(3)-C(4)$  bonds are nearly equal in the static model map (Fig. 6b).

We are grateful to Dr Frode Galsbøl of the H. C. Ørsted Institute, University of Copenhagen, for supplying the crystals.

#### References

- CLEMENTI, E. & RAIMONDI, D. L. (1963). *J. Chem. Phys.* **38**, 2686–2689.  
 EYRING, H., WALTER, J. & KIMBALL, G. E. (1944). *Quantum Chemistry*, pp. 161–163. New York: John Wiley.  
 GALSBOEL, F. (1978). *Acta Chem. Scand. Ser. A*, **32**, 757–761.  
 GALSBOEL, F., STEENBOEL, P. & SØRENSEN, B. S. (1972). *Acta Chem. Scand.* **26**, 3605–3611.  
 HANSEN, N. K. & COPPENS, P. (1978). *Acta Cryst.* **A34**, 909–921.  
 HARNUNG, S. E. & LAIER, T. (1978). *Acta Chem. Scand. Ser. A*, **32**, 41–45.  
 HARNUNG, S. E., SØRENSEN, B. S., CREASER, I., MAEGAARD, H., PFENNINGER, U. & SCHÄFFER, C. E. (1976). *Inorg. Chem.* **15**, 2123–2126.  
 HIRSHFELD, F. L. (1971). *Acta Cryst.* **B27**, 769–781.  
 HOLLADAY, A., LEUNG, P. & COPPENS, P. (1983). *Acta Cryst.* **A39**, 377–387.  
 MIYAMAE, H. (1977). Thesis, Univ. of Tokyo, Japan.  
 MIYAMAE, H., SATO, S. & SAITO, Y. (1977). *Acta Cryst.* **B33**, 3391–3396.  
 MOROOKA, M., OHBA, S., SAITO, Y. & MIYAMAE, H. (1991). *Acta Cryst.* **B47**, 910–917.  
 MOROOKA, M., OHBA, S. & TORIUMI, T. (1992). *Acta Cryst.* **B48**, 459–463.  
 STEWART, R. F., DAVIDSON, E. R. & SIMPSON, W. T. (1965). *J. Chem. Phys.* **42**, 3175–3187.

*Acta Cryst.* (1992). **B48**, 672–677

## Etude des Energies d'Interactions Moléculaires dans la Polymérisation à l'Etat Cristallin du Bis[(*p*-chlorophényl)carbamate] de Hexadiyne-2,4 Diyle-1,6 (1*p*CPU)

PAR PIERRE SPINAT ET CATHERINE BROUTY

Laboratoire de Minéralogie–Cristallographie des Universités Pierre et Marie Curie et Paris VII, associé au CNRS (UA 09), 4 Place Jussieu, Tour 16, 75252 Paris CEDEX 05, France

(Reçu le 23 décembre 1991, accepté le 17 février 1992)

#### Abstract

Conformational and van der Waals interactions have been studied during the solid-state homogeneous polymerization of the urethane diacetylene compound 1*p*CPU ( $C_{20}H_{14}Cl_2N_2O_4$ ). Refinement was

achieved by minimization of all intra- and intermolecular energies (hydrogen-bond energies included), for all monomer and polymer molecules. It is established that the free molecule and the molecule in the crystal adopt different conformations, the first being characterized by a lower energy state